# Design and Implementation of a ZCS Two-Switch Forward Converter with Variable inductor

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Abstract – A zero-current-switching (ZCS) two-switch DC-DC forward converter with variable-inductor is presented in this paper. The quasi-resonant technique is employed to achieve ZCS operation. This variable inductor technique is used to reduce the switching losses and the peak value of the output-diode current. Thus, the conversion efficiency can be improved. Moreover, the voltage across the active switch is clamped at the DC-source input voltage. So, the voltage stress of the active switch is less than that of the conventional DC-DC forward converter. Finally, a prototype circuit is implemented to verify the performance.

Index Terms —two-switch forward converter, variable inductor, ZCS, quasi-resonant

#### I. Introduction

Since power supplies are used widely in the electronic products, large power density is very important. Conventional linear power supplies have some advantages, such as low output ripples, high reliability, and low electro-magnetic interference, but their disadvantages are low power density and low conversion efficiency. Therefore, the switching power supplies are being researched for their ability to increase power density and conversion efficiency. Some switching power supplies utilize pulse-width modulation (PWM) technique, but this approach results in large switching losses [1, 2]. In order to reduce the switching losses, soft-switching techniques, such as resonant and quasiresonant topologies, are developed [3]-[9]. The LC resonant tank is employed for these topologies to achieve zero-current switching (ZCS) or zero-voltage switching (ZVS) for the power devices. Thus, the switching losses can be reduced. However, since the switching frequency of these topologies is not fixed, it will result in higher current stress and conduction losses at the heavy-load condition. Therefore, a variable inductor is used in the resonant tank to adjust the switching frequency for different loads [10]-[13].

A ZCS two-switch DC-DC forward converter is presented in this paper. The variable inductor in the resonant bank is used to reduce the switching losses and peak value of the output-diode current. A prototype circuit with input voltage 400 V, output voltage 48 V, and output power 384 W is implemented to verify the performance.

#### II. OPERATING PRINCIPLES OF THE PROPOSED CONVERTER

Fig. 1 shows the circuit configuration of the proposed converter, which consists of two switches ( $S_1$  and  $S_2$ ), one transformer, four diodes ( $D_1$ ,  $D_2$ ,  $D_0$  and  $D_f$ ), one resonant tank ( $L_r - C_r$ ), one output inductor ( $L_o$ ), and one output capacitor ( $C_o$ ). Switches  $S_1$  and  $S_2$  are controlled by the same gate-drive signal. Variable inductor  $L_r$  is employed for the resonant inductor. The resonant tank is used to achieve ZCS when the switches are turned off. The switching frequency is varied to regulate the output voltage. The turns ratio of transformer n is equal to  $N_s/N_p$ .

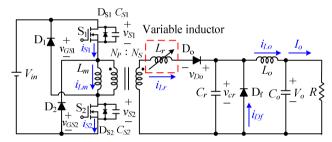


Fig. 1. Circuit configuration of the proposed converter.

In order to simplify the analysis, the following assumptions are made:

- The leakage inductor and the stray capacitor of the transformer are neglected.
- The output inductor is large enough that the current through the output inductor can be treated as constant during one switching period.
- The output capacitor is large enough that the voltage across the output capacitor can be treated as constant during one switching period.
- The output inductor and output capacitor are larger than the resonant inductor and resonant capacitor.
- All the components are ideal.

The key waveforms of the proposed converter are shown in Fig. 2. The operating principle of the proposed converter is described as follows.

## Mode I $[t_0, t_1]$ :

At  $t = t_0$ ,  $S_1$  and  $S_2$  are turned on. The current-flow path is shown in Fig. 3(a). The DC-source energy is transferred to

the resonant tank via the transformer. Meanwhile,  $v_{cr}$  is equal to zero. So, the voltage across  $L_r$  is given as

$$v_{Lr}(t) = nV_{in} = L_r \frac{di_{Lr}(t)}{dt}$$
 (1)

Since  $i_{Lr}$  is equal to  $I_o$  at  $t = t_1$ , the following equation is obtained as

$$nV_{in} = \frac{L_r I_o}{t_1 - t_0} \tag{2}$$

Thus, the duration  $[t_0, t_1]$  is found to be

$$t_1 - t_0 = \frac{L_r I_o}{n V_{in}} \tag{3}$$

## Mode II $[t_1, t_2]$ :

At  $t = t_1$ ,  $S_1$  and  $S_2$  are still turned on. The current flow path is shown in Fig. 3(b). The resonant tank starts to resonate between  $L_r$  and  $C_r$ , and the following exist:

$$v_{cr}(t) = nV_{in} - L_r \frac{di_{Lr}(t)}{dt}, \quad t_1 \le t \le t_2$$
 (4)

$$i_{cr}(t) = i_{Ir}(t) - I_{o}, \quad t_1 \le t \le t_2$$
 (5)

Substituting  $i_{Lr}(t_1) = I_o$  into (4) and (5),  $i_{Lr}$  and  $v_{cr}$  are found to be

$$v_{cr}(t) = nV_{in}[1 - \cos\omega(t - t_1)], \quad t_1 \le t \le t_2$$
 (6)

$$i_{Lr}(t) = I_o + \frac{nV_{in}}{Z_n} \sin \omega (t - t_1), \quad t_1 \le t \le t_2$$
 (7)

where  $\omega = 1/\sqrt{L_r C_r} = 2\pi f_r$  and  $Z_n = \sqrt{L_r / C_r}$ .

From (6) and (7), the peak values of  $v_{cr}$  and  $i_{Lr}$  are derived as

$$V_{cr peak} = 2nV_{in}$$
 (8)

$$I_{Lr\_peak} = I_o + \frac{nV_{in}}{Z_n} \tag{9}$$

Fig. 2 shows that  $i_{Lr}$  is equal to zero at  $t = t_2$ . Substituting  $i_{Lr}(t_2) = 0$  into (7) yields the following:

$$I_o + \frac{nV_{in}}{Z_n} \sin \omega (t_2 - t_1) = 0$$
 (10)

Therefore, the duration  $[t_1, t_2]$  is given by

$$t_2 - t_1 = \frac{1}{\omega} \sin^{-1} \left( -\frac{I_o Z_n}{n V_{in}} \right) \tag{11}$$

## Mode III $[t_2, t_3]$ :

At  $t = t_2$ ,  $S_1$  and  $S_2$  are still turned on. The current-flow path is shown in Fig. 3(c). Meanwhile, there is no energy stored in  $L_r$ . The energy stored in  $C_r$  is delivered to  $L_o$ ,  $C_o$ , and the load. Thus,  $i_{cr}$  is given as

$$i_{cr}(t) = C_r \frac{dv_{cr}(t)}{dt} \tag{12}$$

## Mode IV $[t_3, t_4]$ :

At  $t = t_3$ ,  $S_1$  and  $S_2$  are turned off. The current-flow path is shown in Fig. 3(d). The energy of the DC-source and  $L_m$  are transferred to  $C_{S1}$  and  $C_{S2}$ . The energy stored in  $C_r$  is still discharged to  $L_o$ ,  $C_o$ , and the load. At  $t = t_4$ ,  $v_{cr}$  is equal to zero, and this mode ends. Since  $i_{cr}$  is equal to  $I_o$  at this time interval  $[t_2, t_4]$ , (12) can be rewritten as

$$I_o = \frac{C_r v_{cr}(t_2)}{t_4 - t_2} \tag{13}$$

At  $t = t_2$ , (6) can be represented as

$$v_{cr}(t_2) = nV_{in}[1 - \cos\omega(t_2 - t_1)] \tag{14}$$

So, the duration  $[t_2, t_4]$  is obtained as

$$t_4 - t_2 = \frac{nC_r V_{in}}{I} [1 - \cos \omega (t_2 - t_1)]$$
 (15)

## Mode V $[t_4, t_5]$ :

During this mode,  $S_1$  and  $S_2$  are still turned off. The current-flow path is shown in Fig. 3(e). The energy of the DC-source and  $L_m$  are still transferred to  $C_{S1}$  and  $C_{S2}$ . The energy stored in  $L_o$  is released to  $C_o$  and the load. When the voltages across  $C_{S1}$  and  $C_{S2}$  are equal to  $V_{in}$  at  $t = t_5$ , this mode ends.

## Mode VI $[t_5, t_6]$ :

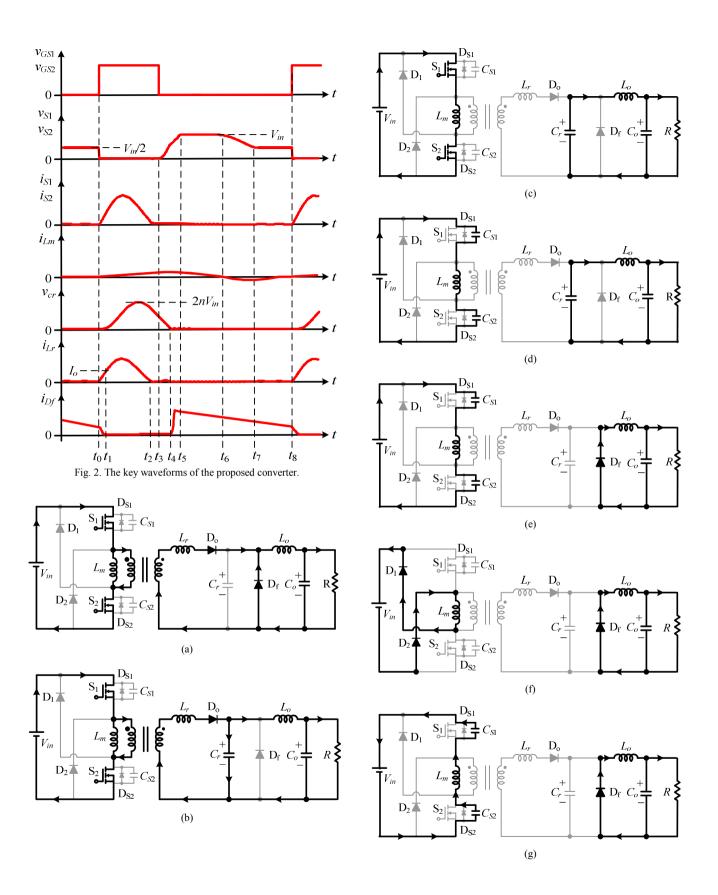
At this mode,  $S_1$  and  $S_2$  are still turned off. The current-flow path is shown in Fig. 3(f). The energy stored in  $L_m$  is entirely released to the DC-source through  $D_1$  and  $D_2$  and the voltages across  $S_1$  and  $S_2$  are clamped at  $V_{in}$ . The energy stored in  $L_o$  is still released to  $C_o$  and the load.

#### Mode VII $[t_6, t_7]$ :

At this mode,  $S_1$  and  $S_2$  are still turned off. The current flow path is shown in Fig. 3(g). Since the energy stored in  $L_m$  is released to empty at  $t = t_0$ , the energies stored in  $C_{S1}$  and  $C_{S2}$  are discharged to  $L_m$  and the DC-source. The energy stored in  $L_o$  is still released to  $C_o$  and the load. When the voltages across  $C_{S1}$  and  $C_{S2}$  are equal to  $0.5V_{in}$  at  $t = t_7$ , this mode ends

## Mode VIII $[t_7, t_8]$ :

At this mode,  $S_1$  and  $S_2$  are still turned off. The current-flow path is shown in Fig. 3(h). The energy stored in  $L_m$  is released to the DC source through  $D_{S1}$  and  $D_{S2}$  until  $i_{Lm}=0$ . The energy stored in  $L_o$  is still released to  $C_o$  and the load. Then, the next switching period begins.



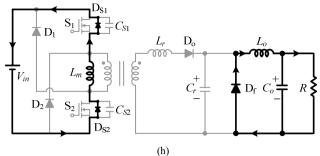


Fig. 3. Current flow path of operating modes during one switching period.

III. STEADY-STATE ANALYSIS OF THE PROPOSED CONVERTER

Assuming all device components are ideal, the input energy is given as

$$W_{in} = \int_0^{t_3} V_{in} i_{in} dt = n V_{in} I_o \left[ \frac{1}{2} (t_1 - t_0) + (t_2 - t_1) + (t_4 - t_2) \right]$$
 (16)

The output energy is derived as

$$W_{o} = \int_{0}^{T_{S}} V_{o} I_{o} dt = V_{o} I_{o} T_{S}$$
 (17)

From (16) and (17), the output voltage  $V_o$  is found to be

$$V_o = \frac{nV_{in}}{T_S} \left[ \frac{1}{2} (t_1 - t_0) + (t_2 - t_1) + (t_4 - t_2) \right]$$
 (18)

Substituting (3), (11) and (15) into (18) yields

$$V_{o} = \frac{nV_{in}}{T_{S}} \left\{ \frac{L_{r}I_{o}}{2nV_{in}} + \frac{1}{\omega} \sin^{-1}(-\frac{I_{o}Z_{n}}{nV_{in}}) + \frac{C_{r}nV_{in}}{I_{o}} \left[ 1 - \cos\omega(t_{2} - t_{1}) \right] \right\}$$
(19)

The normalized parameters are defined as follows:

Normalized voltage: 
$$V_n = \frac{V_o}{nV_{in}}$$
 (20)

Normalized frequency: 
$$f_n = \frac{f_s}{f_r}$$
 (21)

Normalized impedance: 
$$r_n = \frac{R}{Z_n}$$
 (22)

Substituting (20) - (22) into (19) yields following equation:

$$V_{n} - \frac{f_{n}}{2\pi} \left\{ \frac{V_{n}}{2r_{n}} + \sin^{-1}(\frac{-V_{n}}{r_{n}}) + \frac{r_{n}}{V_{n}} \left[ 1 + \sqrt{1 - (\frac{V_{n}}{r_{n}})^{2}} \right] \right\} = 0 \quad (23)$$

The relationship between normalized output voltage  $V_n$  and normalized switching frequency  $f_n$  is shown in Fig. 4. When

parameters  $V_n$ ,  $f_n$ , and  $Z_n$  are selected, the switching frequency can be regulated to control the output voltage.

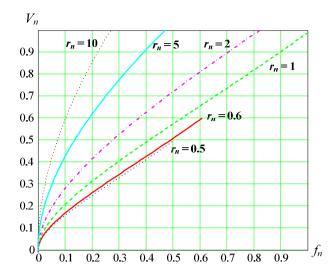


Fig. 4. Normalized output voltage  $V_n$  versus normalized switching frequency  $f_n$ .

#### IV. EXPERIMENTAL RESULTS

A laboratory prototype circuit is implemented to illustrate the performance of the proposed converter. The circuit specifications and parameters are selected to be  $V_{in} = 400 \text{ V}$ ,  $V_o = 48 \text{ V}$ ,  $P_o = 384 \text{ W}$ , n = 0.2,  $f_{s,max} = 100 \text{ kHz}$ , and  $C_r = 220 \text{ nF}$ . Moreover, the power devices are chosen as  $S_1/S_2$ : STP20NM60,  $D_1/D_2$ : UF4006, and  $D_0/D_1$ : MBR20200CT.

Fig. 5 shows the control circuit of the variable-inductor. Resistor  $R_X$  is used to detect the output current and the comparator detects the voltage drop on  $R_X$ . If the output current is larger than 4 A, the output level of the comparator decreases to a low level. Then, switch  $S_X$  is turned off. Thus, the inductance of  $L_r$  can be adjusted as shown in Fig. 6.

Figs. 7 and 8 show some experimental waveforms at the full-load condition,  $P_o = 384$  W. As shown in Fig. 7, switch  $S_1$  is turned off at  $i_{S1} = 0$ . Thus, ZCS operation of the proposed converter is achieved. Fig. 8(a) depicts that when the inductance of  $L_r$  is variable,  $f_s$  is 106 kHz and the peak value of  $i_{Lr}$  is 22 A. Fig. 8(b) shows that  $f_s$  is 129 kHz and the peak value of  $i_{Lr}$  is 25.6 A under  $L_r = 3.2 \mu H$ . Thus, the variable-inductor technique can effectively reduce the switching losses and peak value of output-diode current. Fig. 9 shows the measured efficiency, and it is clear that the variable-inductor technique is better than the fixed-inductance technique at heavy-load conditions. Also, the maximum efficiency of the proposed converter is 93.3 % at  $P_o = 288$  W.

## V. CONCLUSIONS

A ZCS two-switch DC-DC forward converter with variable inductor is researched in this paper. The proposed converter employs a quasi-resonant technique to achieve ZCS

operation. A variable-inductor technique is used to reduce the switching losses and peak value of the output-diode current, and the extra third winding in the transformer is not required. The residual energy of the transformer can be delivered to the DC source. Moreover, the voltages across switches  $S_1$  and  $S_2$  can be clamped at DC-source voltage  $V_{in}$ . Finally, a prototype circuit is implemented. Experimental results shown that the maximum efficiency is 93.3 % at  $P_o = 288$  W.

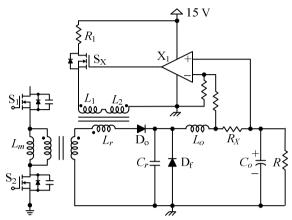
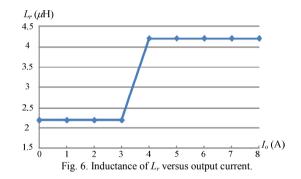
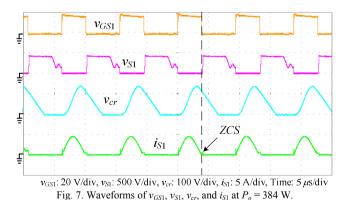
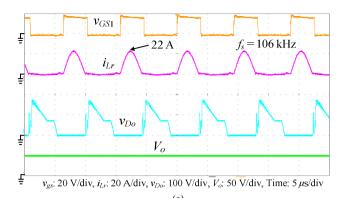


Fig. 5. Control circuit of variable inductor.







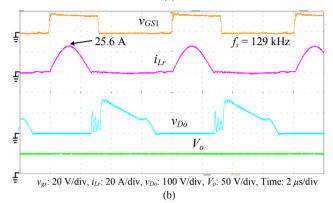
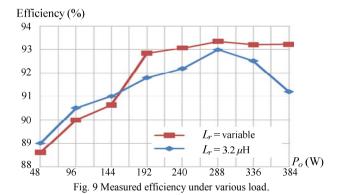


Fig. 8 Waveforms of  $v_{GS1}$ ,  $i_{Lr}$ ,  $v_{Do}$ , and  $V_o$  at  $P_o = 384$  W: (a) variable inductance  $L_r$ , (b)  $L_r = 3.2~\mu\text{H}$ .



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